

**A Shared Memory Algorithm and Proof  
for the Alternative Construct in CSP**

*Richard M. Fujimoto  
Hwa-chung Feng*

DEPARTMENT OF COMPUTER SCIENCE  
UNIVERSITY OF UTAH

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A Shared Memory Algorithm and Proof  
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Richard M. Fujimoto<sup>1</sup>  
Hwa-chung Feng

Department Of Computer Science  
University Of Utah  
Salt Lake City, UT 84112

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## Abstract

Communicating Sequential Processes (CSP) is a paradigm for communication and synchronization among distributed processes. The alternative construct is a key feature of CSP that allows nondeterministic selection of one among several possible communicants. Previous algorithms for this construct assume a message passing architecture and are not appropriate for multiprocessor systems that feature shared memory. This paper describes a distributed algorithm for the alternative construct that exploits the capabilities of a parallel computer with shared memory. The algorithm assumes a generalized version of Hoare's original alternative construct that allows output commands to be included in guards. A correctness proof of the proposed algorithm is presented to show that the algorithm conforms to some *safety* and *liveness* criteria. Extensions to allow termination of processes and to ensure fairness in guard selection are also given.

Keywords: communicating sequential processes; alternative operation; shared memory multiprocessor; parallel processing.

# 1 Introduction

Communicating Sequential Processes (CSP) is a well known paradigm for communication and synchronization of a parallel computation [11,10]. A CSP program consists of a collection of processes  $P_1, P_2, \dots, P_N$  that interact by exchanging *messages*. These message passing primitives, called input and output commands, are synchronous — a process attempting to output (input) a message to (from) another process must wait until the second process has executed the corresponding input (output) primitive.

An important feature of CSP is the *alternative* construct which is based on Dijkstra's guarded command[6]. This construct enables a process to *nondeterministically* select one communicant among many. Each alternative operation specifies a list of guards. Each guard has a set of actions associated with it that cannot be executed until the value of the corresponding guard becomes TRUE. Each guard consists of a sequence of boolean expressions and an optional input command (output guards were not allowed in the original specification of CSP). A guard is said to be *enabled* if each of the boolean expressions preceding the input command evaluates to TRUE. The value of a guard is TRUE if the guard is enabled and its input action has successfully completed.

Implementation of the alternative construct on a multiple processor computer has been the subject of much research [1,2,3,4,5,12,15,22]. It has been argued that the exclusion of output guards in the original definition of CSP is too restrictive and sometimes degrades performance [3,15]. Algorithms that allow output guards in the alternative construct have been proposed[1,2,3,4]. Others suggest a paradigm similar to that which was originally proposed [9,12,22]. All of the algorithms reported thus far assume a message-based computer architecture; no shared memory is assumed. The principal contribution of this paper is to present an algorithm for implementing the alternative construct on a shared memory multiprocessor and to prove its correctness. To the authors' knowledge, no such algorithm has previously been reported.

CSP does not assume shared memory between constituent processes, so one might ask why implementation on a shared memory machine is an issue. Implementation of CSP on a shared memory architecture is an important question for several reasons:

- CSP has clean semantics that simplify proving the correctness of programs. It is a worthwhile programming paradigm in its own right, independent of the underlying machine architecture.
- The message passing paradigm is a natural means of expressing programs in many applications areas that are well suitable for shared memory machines. For example, distributed discrete event simulation algorithms are usually described in terms of message passing paradigms [13, 16], and implementations on shared memory architectures have been described [21]. Similarly,

message passing is used extensively in object-oriented programming.

- Shared memory machines are widely available. Multiprocessors such as the BBN Butterfly<sup>TM</sup> [23] and Sequent Balance<sup>TM</sup> are available from the commercial sector, and numerous shared memory research machines such as IBM's RP3 [18] and the University of Illinois's Cedar [8] have also been developed.
- Shared memory architectures provide fast interprocessor communications. A complete interconnection among processors is provided, avoiding costly store-and-forward communication software in message-based architectures such as the Intel iPSC<sup>TM</sup> [20]. At present, parallel processors using shared memory are more appropriate for applications requiring frequent communication among the constituent processes.

Although one can clearly “retrofit” any message-based algorithm to a shared memory architecture by building a suitable interface, this will often lead to an inappropriate and awkward implementation. Existing message-based algorithms for the alternative construct are not appropriate for a shared memory machine because (1) they do not exploit the facilities afforded by shared memory, leading to an inefficient implementation; and (2) they require additional “system” processes to respond to incoming messages (e.g., requests for rendezvous) resulting in unnecessary context switching overhead. We will describe an algorithm for the CSP alternative construct that exploits the facilities afforded by shared memory and avoids the aforementioned system processes. This algorithm implements the “generalized” alternative construct that allows output guards.

The proposed algorithm uses the notion of total ordering among processes [3] to prevent deadlocks, but applies this principle *dynamically* on transactions (defined later) rather than statically as originally proposed. The shared memory architecture simplifies the task of maintaining globally unique IDs. The status of a remote process can be interrogated directly, in contrast to the message-based algorithms where message handshake and context switching overheads reduce the efficiency of the implementation. However, because processes in the proposed algorithm concurrently access shared data, great care must be taken to avoid race conditions. Therefore, we provide a proof of the correctness of the algorithm according to *safety* and *liveness* criteria [14]. Modifications are also suggested to achieve fairness [7].

Finally, the algorithm does not contain any inherent *hot spots* [19]. The few global variables that are shared by all processes are not accessed with sufficient frequency to constitute a hot spot. With the exception of these global variables, the algorithm is fully distributed and does not rely on any centralized controller.

The remainder of this paper is organized as follows. The semantics of the generalized alternative

construct are discussed first, followed by a description of the assumed machine architecture. The proposed algorithm and a discussion of its operation is then presented. Other important issues related to the algorithm are then discussed, and an extension to handle termination of processes is described. We conclude the paper with a proof of the correctness of the algorithm followed by a discussion of fairness issues.

## 2 The Alternative Construct

A guard of the alternative construct can appear in one of two possible forms. The first, called the *pure boolean* form, contains no I/O command. For example, in

$$(x = 1 \text{ and } y > 5) \rightarrow z := z * 3;$$

the predicate to the left of the ' $\rightarrow$ ' operator is a pure boolean guard. The second form, called the *I/O guard* form, contains an I/O command as well as an (optional) boolean part. For example, in

$$P_1?x \rightarrow z := z + 1;$$

the input guard  $P_1?x$  requests input from process  $P_1$ . The received data is assigned to the variable  $x$ . Guards such as this which do not contain a boolean part are referred to as *pure I/O guards*. In effect, the boolean part is the constant TRUE. An I/O guard is said to be *enabled* if the boolean part is TRUE, so a pure I/O guard is *permanently* enabled.

Consider the following alternative construct:

$$[G_{i(i \in PB)} \rightarrow S_i \square G_{j(j \in IO)} \rightarrow S_j].$$

Where  $PB$  stands for the set of indices of all of the pure boolean guards and  $IO$  the set of indices of all of the I/O guards. Whenever this alternative construct is executed, exactly one guard is selected and the corresponding action ( $S_i$  or  $S_j$ ) is executed. The selection is made according to the *availability* of the guards. For pure boolean guards, the guard is said to be available if it is enabled, i.e., if the boolean part evaluates to TRUE. For I/O guards, the guard is available if it is enabled and the process associated with the guard is also ready to communicate using the complementary I/O command. Because we assume I/O commands only appear in guards of alternative operations, this implies the remote process is executing an alternative operation in which the corresponding I/O operation is part of an enabled guard. If more than one guard is available, one is chosen arbitrarily. The application program cannot control this selection.

Pure boolean guards can be resolved without any interaction with other processes. Therefore, to simplify the discussion which follows, we will restrict attention to the resolution of I/O guards.

### 3 The Machine Architecture

The machine is assumed to be a shared memory multiprocessor. The algorithm is well suited for machines such as BBN's Butterfly or Sequent's Balance, among others. Several primitives are used in the algorithm. None are unusual in a multiprocessor environment, and all can be easily constructed using a test-and-set and standard scheduling primitives.

The CSP program contains processes  $P_1, P_2, \dots, P_N$ . Process  $P_i$  is assigned the unique *process ID*  $i$  to distinguish it from others.

We will assume the following:

- Communications are reliable. An error free communications mechanism exists so that two distinct processes can communicate by exchanging a message. In particular, **Send**( $M, R$ ) and **Recv**( $R$ ): **Message** provide the same semantics as CSP's output and input commands, respectively.  $M$  is the message which is transmitted and  $R$  is the ID of the remote process with which communications is to take place. *Recv* returns the received message (of type *Message*). In accordance with CSP semantics, we assume the process invoking the primitive blocks until process  $P_R$  executes the complementary I/O primitive.
- Read and write accesses to shared memory are atomic, as is normally the case with a shared memory multiprocessor. **AtomicAdd**( $X$ ): **INTEGER** atomically increments the integer variable  $X$  and returns the original value of  $X$ .
- *WaitForSignal* and *Signal* primitives are available to block and unblock the process, respectively. A signal contains a single, user defined integer value. **WaitForSignal**( $i$ ): **INTEGER** causes the process invoking the primitive to block until a signal becomes available to it from *any* other process and returns the integer value stored within the signal. **Signal**( $R, i$ ) sends a signal containing integer  $i$  to process  $P_R$ . The *Signal* primitive wakes up the signaled process if it is blocked on *WaitForSignal*. Otherwise, the signal remains in effect until  $P_R$  executes a *WaitForSignal* primitive. If a second signal is sent to  $P_R$  before the first is absorbed by a call to *WaitForSignal*, the first signal is discarded.
- *Lock* and *Unlock* primitives provide exclusive access to shared data structures. **Lock**( $L$ ) will block until the lock  $L$  becomes zero, at which time  $L$  is set to one. The "test-and-set" operation must be atomic. **Unlock**( $L$ ) sets the lock  $L$  to zero. Further, we assume the *Lock* primitive is fair, i.e., if a process is blocked while attempting to obtain a lock, it does not remain blocked an unbounded amount of time unless the lock is not unlocked for an unbounded amount of time.

- **Sleep( $T$ )** causes the process invoking it to block for at least  $T$  time units. A process will always eventually awake after calling *Sleep*.
- The amount of time between successive samples of a shared memory location by a busy wait loop (which does nothing but sample and test the value stored in this location for inequality) can be bounded, and is shorter than the time required to invoke either the *Send* or *Recv* primitives defined above.

This final “timing” assumption is perhaps the most distasteful aspect of the proposed algorithm. It is not necessary to ensure the safety of the algorithm, i.e., if it were relaxed, no “invalid” rendezvous will result. The assumption is primarily a theoretical requirement that is necessary to prove liveness and has only limited practical implications. If this assumption is relaxed, specific scenarios requiring a prolonged, highly synchronous behavior between independent processes must develop to violate liveness. Such scenarios are unlikely to occur in practice, as will be discussed in detail after the algorithm has been described, and precautions can be taken to reduce the likelihood of such occurrences if the timing assumption cannot be guaranteed.

It is assumed that all input and output commands occur within guards of the alternative construct. Simple CSP input and output primitives are special cases of the alternative construct. We also assume that the variables used in the alternative algorithm are not modified by processes except as indicated in the algorithm. Finally, it is assumed that processes do not terminate. The algorithm can be extended to handle termination, as will be discussed later.

## 4 The Alternative Algorithm

Each invocation of an alternative operation is referred to as a *transaction*. A transaction begins when an alternative operation is initiated and ends when a successful communication has been completed. A process will usually engage in many transactions during its lifetime. A total ordering is imposed among all transactions entered by *all* processes of a given CSP program. A unique sequence number, referred to here as a *transaction ID*, is associated with each transaction.

Two processes which each initiates an alternative operation that results in a communication between them are said to *rendezvous*. More precise definitions of rendezvous and other terminology introduced in this section will be presented later. Each rendezvous always involves exactly two distinct processes. In a *typical* rendezvous, the first process to enter the alternative will block, waiting for a signal from the second. When the second process enters the alternative, it will *commit* to the first in order to obtain “permission” to rendezvous; the “committing” process will then signal and exchange a message with the blocked process, and both will complete their respective



alternative operations.

A *commit* operation is, in effect, a request for rendezvous. It will be shown that a rendezvous will occur only after a successful commit operation has taken place, and every successful commit results in a rendezvous. A process will not attempt to commit until it has determined that the process with which it is committing is a suitable candidate for rendezvous, i.e., each lists the other in their respective guard lists, and the two processes are not both trying to execute the *same* I/O operation (*Send* or *Recv*). The commit operation resolves conflicts when two different processes attempt to simultaneously rendezvous with a third. The algorithm uses an “abort and retry” mechanism to avoid race conditions when two potential communicants simultaneously enter the alternative command.

#### 4.1 Process States

Each process can be in one of the following states:

- **WAITING.** The process is blocked on a *WaitForSignal* operation, waiting for another process to rendezvous with it.
- **ALT.** The process has begun an alternative operation, and is scanning through its list of guards to find a process with which it can rendezvous.
- **SLEEPING.** The process was forced to abort an alternative operation. After aborting, the process goes to sleep for some predetermined period of time before retrying. While blocked in this way, the process is in the **SLEEPING** state. This state differs from the **WAITING** state because a process may remain in the latter for an unbounded amount of time.
- **RUNNING.** The process is executing user or system code not related to the alternative operation. The process is in the **RUNNING** state if it is not in any of the other states listed above. Once the process initiates an alternative operation, it can only be in the **WAITING**, **ALT**, or **SLEEPING** state until the alternative operation completes with a rendezvous.

It is possible to combine the **RUNNING** and **SLEEPING** states into a single state. Two states are used to simplify the description of the algorithm and its proof.

A state transition diagram for each process is shown in figure 1. Initially, a process is in the **RUNNING** state. Once the process initiates an alternative operation, it enters the **ALT** state. If the process is forced to abort the alternative it switches to the **SLEEPING** state, and returns to the **ALT** state when it retries. If the process is able to commit and rendezvous with another process,

it returns to the `RUNNING` state. Otherwise, the process moves to the `WAITING` state until some other process commits to it, at which time it rendezvous and returns to the `RUNNING` state.

The `ALT` and `SLEEPING` states should be viewed as “transitory” states through which a process must pass while trying to commit or move into the `WAITING` state. It will be shown that a process cannot remain in either the `ALT` or the `SLEEPING` state for an unbounded amount of time on a single transaction.

## 4.2 Shared Variables

Each process  $P_j$  maintains a number of variables that may be examined, and in some cases modified, by other processes:

- **AltList<sub>j</sub>** lists the guards associated with the last alternative operation initiated by  $P_j$  that caused  $P_j$  to enter the `WAITING` state.
- **AltLock<sub>j</sub>** is a lock used to control access to *AltList<sub>j</sub>*. It is initialized to 0 (unlocked).
- **State<sub>j</sub>** holds the current state of  $P_j$ . It may be set to `WAITING`, `ALT`, `SLEEPING`, or `RUNNING`, and is initialized to `RUNNING`.
- **WakeUp<sub>j</sub>** is initialized to 1 and is set to zero by  $P_j$  whenever it enters the `WAITING` state. It is incremented (atomically) by processes trying to commit to  $P_j$ . This variable prevents two processes from both successfully committing to a third on a single transaction.

There is also one system wide global variable used by the algorithm:

- **NextTransID** is initialized to zero and is incremented each time a process initiates an alternative operation. This variable ensures a unique transaction ID can be generated for each instance of an alternative operation.

One procedure merits special attention. **CheckAndCommit(AltList<sub>r</sub>, g<sub>i</sub>): INTEGER** is called by process  $P_l$  ( $l$  denotes the *local* process) to check that “valid” communications can take place between  $P_l$  using guard  $g_i$  and  $P_r$  ( $r$  denotes the *remote* process), and if so, to attempt to commit to  $P_r$ . If a commit was attempted and succeeded, then *CheckAndCommit* returns a positive integer indicating the corresponding guard in the *remote* process  $P_r$ . Otherwise, *CheckAndCommit* returns a non-positive integer, denoted by the constant `FAILED`. This procedure is shown in figure 2.

*CheckAndCommit* uses a procedure **CheckGuard(AltList<sub>r</sub>, g<sub>i</sub>): INTEGER** that scans the remote alternative list *AltList<sub>r</sub>*, looking for a *matching* and *compatible* guard  $g_j$  to the local guard  $g_i$ . By *matching* we mean  $g_j$  contains an I/O operation with  $P_l$ . By *compatible* we mean  $g_i$  and  $g_j$  do

not *both* contain input (output) commands. *CheckGuard* returns  $j$ , the number of a matching and compatible guard if one was found, and **FAILED** otherwise. If such a guard is found,  $P_l$  attempts to commit to  $P_r$  by testing if  $WakeUp_r$  is zero, and if so, incrementing it. An ordinary addition is used rather than the *AtomicAdd* primitive to increment  $WakeUp_r$  because *AltLock\_r* guarantees atomicity — every “test-and-set” operation performed on  $WakeUp_r$  occurs while *AltLock\_r* is set. If  $P_l$  is the first process to commit to  $P_r$ , i.e., if  $WakeUp_r$  was previously zero, then  $P_l$  successfully commits, *CheckAndCommit* returns the number of the corresponding guard, and rendezvous is imminent. Otherwise, *CheckAndCommit* returns **FAILED**. *AltLock\_r* ensures serial access to *AltList\_r*. As will be demonstrated later, it is crucial that this lock is not released until *after* the commit operation is attempted (if it is attempted) in order to avoid race conditions. This would be the case even if an *AtomicAdd* operation were used to increment the *WakeUp* variable.

### 4.3 Other Notation

For notational convenience, other variables and predefined functions are defined that are used in the algorithm. These include:

- **TransID<sub>l</sub>** is a variable that contains the ID of the current transaction in which process  $P_l$  is engaged.
- **CommunicantID( $g_i$ )** is a function that returns the ID of the process listed in the I/O command portion of guard  $g_i$ .
- **Communicate( $g_i$ )** executes the I/O command in guard  $g_i$ .
- **TimeOut** is a constant indicating the number of time units a process should sleep after an aborted attempt. More will be said about this later.

### 4.4 Description Of The Algorithm

The alternative algorithm is shown in figures 3 and 4. The *Alternative* procedure shown in figure 3 is a “front end” that is responsible for retrying aborted attempts. The heart of the algorithm lies in the *TryAlternative* procedure shown in figure 4. The parameters passed to both procedures are  $n$  enabled I/O guards  $g_1, g_2, \dots, g_n$ . Each guard contains either a single output or a single input primitive. The *Alternative* procedure is only called after non I/O guards have been evaluated and are found to be **FALSE**. This procedure does not return until a rendezvous has been completed at which time it returns an integer indicating the guard ( $g_1, g_2, \dots, g_n$ ) that was eventually satisfied.

The *Alternative* procedure obtains a unique transaction ID by performing an *AtomicAdd* operation on the global *NextTransID* variable. It then attempts to rendezvous by calling *TryAlternative*. *TryAlternative* either returns the number of the guard on which a rendezvous occurred, or the FAILED flag indicating the attempt must be retried. Each time *TryAlternative* fails, the process enters the SLEEPING state for at least *TimeOut* time units before retrying. The same transaction ID remains in use despite one or more failed attempts. It will be shown that *TryAlternative* cannot fail an unbounded number of times within a single transaction.

The heart of the alternative algorithm is embodied in the *TryAlternative* procedure (figure 4). In this procedure,  $l$  refers to the local process  $P_l$ , and  $r$  refers to the remote process  $P_r$  associated with the guard that is being scanned.

After setting the state of the process to ALT,  $P_l$  examines each guard listed in the alternative operation one after the other. Some action is then performed depending on the state of  $P_r$ .

If  $P_r$  is in the RUNNING state,  $P_l$  simply advances to the next guard. In this case,  $P_r$  has not yet entered a transaction and is not yet ready to rendezvous.

If  $P_r$  is in the SLEEPING state,  $P_l$  again advances to the next guard.  $P_l$  advances because the *Alternative* procedure guarantees that the SLEEPING process ( $P_r$ ) will eventually retry its alternative operation. If  $P_l$  and  $P_r$  are destined to eventually rendezvous on this transaction,  $P_l$  will typically proceed to the WAITING state, and  $P_r$  will later retry, commit, and rendezvous with  $P_l$ .

If  $P_r$  is WAITING, then  $P_r$  has already reached the rendezvous point so  $P_l$  attempts to rendezvous. *AltList<sub>r</sub>* is examined to make sure a valid communication can take place, and if so,  $P_l$  attempts to commit. If successful,  $P_l$  will awaken  $P_r$  (by sending a signal) and rendezvous. Otherwise,  $P_l$  advances to the next guard.

Finally, if  $P_r$  is in the ALT state, some special precautions must be taken to avoid race conditions. This situation could result, for example, when  $P_l$  and  $P_r$  initiate an alternative operation at approximately the same time. The two processes may or may not be destined to rendezvous, however. In fact,  $P_r$ 's alternative operation may not even contain a guard with  $P_l$  as a communicant.

If two processes see each other in the ALT state, one will be forced to abort and retry the alternative, while the other pauses within the current operation until the first aborts. The transaction IDs of the two processes are used to determine the process that will abort and the process that will proceed. A process with a smaller, i.e., older, transaction ID is given higher priority. This protocol avoids deadlock situations in which two processes attempting to communicate with each other both advance to the WAITING state.

If the process does not abort, it pauses in a busy wait loop until the remote process moves out of the ALT state. The remote process will either abort, changing to the SLEEPING state, or rendezvous,

changing to the `RUNNING` state. Later, it will be shown that one of these two possibilities must eventually occur. Although the busy wait loop and abort retry scenario might initially appear to cause wasted time that could be better spent pursuing other activities, it is anticipated that this situation will arise infrequently in practice. Performance evaluations using empirical techniques are currently in progress to verify that this is the case.

It is interesting to note that the state of  $P_r$  may change immediately after  $P_l$  examines  $State_r$ . It will be proven that the algorithm operates correctly despite this potential inconsistency. In fact, it will be shown that the only locking that must be performed in the entire algorithm is that associated with *AltLock*.

If  $P_l$  goes through its entire guard list without rendezvousing with another process,  $P_l$  enters the `WAITING` state and calls *WaitForSignal* to block until another process commits to it. Before calling *WaitForSignal*, however,  $P_l$  also sets  $AltList_l$  to contain the current guard list and “activates”  $WakeUp_l$  by setting it to zero. After some process later commits to  $P_l$ , a signal is received, a communication takes place, and *TryAlternative* returns the identity of the (local) guard that rendezvoused. This information is sent to  $P_l$  in the signal that awakened it.

We should emphasize at this point that it is crucial that the operations listed in figures 2, 3, and 4 be performed in *exactly* the order in which they appear. Seemingly minor changes such as swapping the order of the statements

```
WakeUpl := 0;
Statel := WAITING;
```

introduces a race condition that invalidates the correctness proof.

We note that the *Lock* operation preceding the statement that modifies *AltList* must remain even if modification can be done atomically. The locking protocol in this and the *CheckAndCommit* procedure are carefully designed to avoid race conditions. Finally, it is noteworthy that the statement that sets  $WakeUp_l$  to zero need *not* be executed while *AltLock<sub>l</sub>* is locked. The correctness proof only requires that two processes do not both read a zero value from  $WakeUp_l$  during a single transaction of  $P_l$ . This is guaranteed by the locking protocol used in *CheckAndCommit*.

## 5 Discussion

Several aspects of the alternative algorithm presented above merit further discussion. These are discussed next.

## 5.1 Transaction IDs

The algorithm uses dynamically assigned transaction IDs to determine the “winner” when a process finds another in the ALT state. Dynamic IDs are used rather than static, process IDs to ensure liveness. Intuitively, *liveness* means that two processes that “should” rendezvous eventually will, while *safety* means that any rendezvous that occurs is valid. The proposed approach avoids scenarios in which a process is repeatedly forced to abort and retry its alternative operation an unbounded number of times; this is because the priority of a transaction automatically increases with time as other transactions are allowed to complete and new ones, with higher IDs and correspondingly lower priorities, are initiated. Dynamic transaction IDs guarantee this property while static IDs do not. It is important that a new transaction ID is only allocated when an alternative is first initiated, as is done in figure 3, and *not* when an existing operation is retried. The use of dynamic transaction IDs is further justified by the fact that global variables are relatively inexpensive in shared memory architectures, and the *NextTransID* variable is not referenced with sufficient frequency to become a hot spot.

A second concern is overflow of the *NextTransID* variable. Overflow invalidates the liveness property of the algorithm because a transaction’s priority does not necessarily increase with time. Also, because transaction IDs cannot be guaranteed to be unique after overflow has occurred, the arbitration protocol could fail (this could be circumvented by appending the process ID to the least significant portion of the transaction ID, however). In any event, overflow can be easily avoided by using a variable of large precision. For example, a 64 bit variable will not overflow with 1000 processes, each initiating a new alternative construct every microsecond, in over 500 years!

## 5.2 The Timing Assumption

We earlier required the following assumption to ensure liveness:

The amount of time between successive samples of a shared memory location by a busy wait loop (which does nothing but sample and test the value stored in this location for inequality) can be bounded, and is shorter than the time required to invoke either the *Send* or *Recv* primitives.

This assumption is necessary because the algorithm uses a polling loop to detect another process leaving the ALT state. Suppose  $P_i$  is waiting for  $P_j$  to change to a new state. It is possible, albeit unlikely, that  $P_j$  (1) modifies  $State_j$ , (2) rendezvous and resumes execution of user code or goes to sleep for *TimeOut* units of time, and (3) reenters *TryAlternative* and changes  $State_j$  back to ALT; all of this must occur *without*  $P_i$  noticing  $State_j$  had been modified, so this activity must

occur *between* successive samples of  $State_j$  by  $P_i$ 's polling loop. While it is true that this might occasionally occur if  $P_i$  is interrupted during its polling loop, it is necessary that this scenario be repeated *an unbounded number of times* within a single execution of the polling loop to compromise the liveness of the algorithm. We conjecture that it is highly improbable that such a scenario will occur even a few times within a single transaction. Further, we emphasize that safety remains guaranteed even if the above assumption is relaxed, so no ill effects, other than delays, will result should this scenario occur some (finite) number of times.

As can be seen from figure 4,  $P_j$  must execute either the *Sleep*, *Send*, or *Recv* primitive *after* the state of  $P_j$  is changed (to SLEEPING or RUNNING), i.e., during step (2) above. Therefore, as stated in the above assumption, ensuring that the minimum execution time of each of these primitives exceeds the time between successive samples of  $P_i$ 's polling loop is sufficient to avoid the above scenario (actually, the *Sleep* primitive is excluded because its minimum execution time is trivially set). If the time between successive samples of the polling loop can be bounded, the minimum amount of time required by the *Send* and *Recv* primitives can be easily modified to adhere to the timing assumption through the introduction of a timed delay (e.g., by calling *Sleep*). However, one would not expect introduction of such a delay to be necessary in most practical situations.

Assuming the time required by a remote memory reference is bounded, the time between successive samples by the busy wait loop can be bounded by disabling interrupts during the polling loop. If this is not a viable alternative, one can reduce the likelihood of entering the above scenario by introducing randomness into the program's temporal behavior. For example, a random sleeping period may be selected (with some minimum value, as described below) when a process is forced to abort. This will reduce the likelihood of excessive delays caused by synchronized behavior between processes.

### 5.3 Setting the Sleeping Period

The "sleep period" before a retry is attempted, i.e., *TimeOut* in figure 4, must be sufficiently long to allow the "winning" process to observe that the sleeping process is indeed in the SLEEPING state. In particular, *TimeOut* cannot be shorter than the interval between successive samples in the busy wait loop executed by the winner.

On the other hand, an excessively long sleeping period will lead to an inefficient implementation. A reasonable *TimeOut* value is the time required for a few remote memory references.

## 5.4 Channel I/O

In many CSP implementations, interprocess communication is based on pre-allocated *channels*. Each channel is a unilateral link between two communicating processes. The channel model facilitates modularity, reusability, and hierarchical construction of programs because a program can be “constructed” by interconnecting a group of constituent processes. The algorithm presented above can be adapted to the channel I/O model by modifying the *Send* and *Recv* primitives and translating port identifiers to process IDs. The *CheckAndCommit* procedure, for instance, must be modified to check for matching *channels* rather than matching process IDs. These modifications are a simple extension of the proposed algorithm.

## 5.5 Termination

Termination is another important issue facing real implementations. This was not treated in the previous discussion because it introduces obscurities into the description. The termination semantics play an important role in CSP because it is the basis of the termination of the *repetitive* command [11]. If an alternative operation is embedded within a repetitive command and no guard of the alternative can become true, e.g., because all processes associated with enabled guards have terminated, the repetitive command terminates. If no such repetitive command surrounds the alternative operation and it is found that no guards can become true, an error results.

In the context of the proposed algorithm, it is sufficient that the *Alternative* procedure determine when no guards can become satisfied and return an appropriate flag denoting this situation. The algorithm can be extended to handle termination by adding a shared variable called *GuardCount<sub>i</sub>*; to each process  $P_i$  and a new process state called TERMINATED. *GuardCount<sub>i</sub>* indicates the number of I/O guards on which  $P_i$  might potentially rendezvous for the current transaction and contains a meaningful value whenever  $P_i$  is in the WAITING state. It is equivalent to the number of guards in *AltList<sub>i</sub>*. The *GuardCount<sub>i</sub>* variable is used to detect situations in which  $P_i$  cannot rendezvous because all of the processes in its guards have terminated. This is the only case in which the *Alternative* procedure will return *without* rendezvous.

Whenever a process  $P_j$  terminates, it marks its state as TERMINATED and then examines the state of each of its neighboring processes, i.e., those processes which might communicate with  $P_j$ . If  $P_j$  finds another process  $P_i$  in the ALT state, it executes a busy wait loop until *State<sub>i</sub>* changes. This is necessary because  $P_j$  cannot know if  $P_i$  saw  $P_j$  had entered the TERMINATED state. If  $P_j$  finds  $P_i$  in the WAITING state and *AltList<sub>i</sub>* contains a guard listing  $P_j$  as a communicant, then  $P_j$  (atomically) decrements *GuardCount<sub>i</sub>* to indicate that one fewer guard is available for rendezvous. No further action is required unless the decrement operation causes *GuardCount<sub>i</sub>* to become zero.



In this case, the terminating process must send  $P_i$  a special signal to indicate  $P_i$ 's alternative operation can never rendezvous. Upon receiving this signal, the alternative operation in  $P_i$  will return a special flag indicating the alternative operation completed *without* rendezvous.

When looking for a process with which to rendezvous, i.e., when scanning the status of neighboring processes in the *TryAlternative* procedure, an I/O guard corresponding to a terminated process is skipped in the same way processes in the RUNNING or SLEEPING state are skipped. Such guards are excluded from *AltList<sub>i</sub>*; and *GuardCount<sub>i</sub>*; should the process fail to rendezvous and move into the WAITING state. If all I/O guards correspond to terminated processes, the alternative construct again returns a flag indicating the operation completed without rendezvous.

Finally, some precautions must be taken to avoid race conditions. The mechanism described above to notify a WAITING process that it cannot rendezvous on any of its guards bears some resemblance to the protocol used to commit to a process — the *WakeUp* variable is analogous to *GuardCount* and committing (by incrementing *WakeUp*) is analogous to decrementing *GuardCount*. Therefore, it is not surprising that the precautions that are necessary to avoid race conditions are similar. In particular, *GuardCount<sub>i</sub>* must be set *before*  $P_i$  sets *State<sub>i</sub>* to WAITING but *after*  $P_i$  modifies *AltList<sub>i</sub>*; (see figure 4). Identical constraints apply regarding the moment at which *WakeUp* to set to zero. Finally, when  $P_j$  wishes to decrement *GuardCount<sub>i</sub>*, the same protocol that was used in the *CheckAndCommit* procedure (see figure 2) to lock *AltLock<sub>i</sub>*; must be used to decrement *GuardCount<sub>i</sub>*, i.e., *AltLock<sub>i</sub>*; must *not* be released until *after* the decrement operation has completed.

## 6 Proof of Correctness

The correctness of the algorithm is established by proving that during the (potentially) infinite execution sequence, all processes and the interplay between them maintain invariant properties known as *safety* and *liveness* [14,17]. As described above, safety means that any rendezvous which occurs is correct. For example, it is not possible for two processes to rendezvous which do not each list the other in some guard of their respective alternative lists. Liveness ensures that two processes which should rendezvous eventually will, provided of course each does not first rendezvous with some other process. These terms are defined more formally in theorems 2 and 3. Intuitively, the safety property ensures that nothing “bad” will happen, while liveness ensures something “good” will eventually happen. Together they guarantee correct operation of the algorithm.

Before beginning the proof, terminology that has been used informally until now will be defined more precisely. These definitions are in terms of the alternative algorithm shown in figures 2, 3, and 4. It is assumed throughout that the CSP program consists of a collection of processes,  $P_1$ ,

$P_2, \dots, P_N$ .

## 6.1 Definitions

1. A process  $P_i$  is said to enter a transaction  $T_r$  when  $P_i$  calls the *Alternative* function. It exits transaction  $T_r$  when it returns from the function call.  $P_i(T_r)$  denotes that fact that  $P_i$  is in  $T_r$ . Each transaction has a unique ID associated with it ( $r$  for transaction  $T_r$ ) that is used to form a total ordering among all transactions. A transaction need not terminate. For example, the *application* program may deadlock.
2. A process  $P_i$  in transaction  $T_r$  is said to *commit* to process  $P_j$  if  $P_i(T_r)$  increments  $WakeUp_j$  from zero to one. The algorithm is such that every time  $WakeUp_j$  is incremented, a commit operation takes place.
3. A transaction  $T_r$  executed by process  $P_i$  is said to rendezvous with transaction  $T_s$  for process  $P_j$  if either (a)  $P_i$  is in the **WAITING** state and receives a signal from  $P_j$ , or (b)  $P_i$  signals  $P_j$  after committing to  $P_j$ . It will be shown that once a process rendezvous, it will exchange a message, complete the current transaction and return to the **RUNNING** state.
4. A signal sent by  $P_i$  to  $P_j$  is said to be *pending* if (1) it was sent but has not yet been received by  $P_j$ , or (2) it was received, but has not yet been absorbed by  $P_j$  through a call to *WaitForSignal*.
5. A communication between  $P_i$  and  $P_j$  is *compatible* if one process wishes to send, and the other wishes to receive. Otherwise, the communication is said to be *incompatible*.
6.  $VAR_i(T_r)$  denotes the value of state variable  $VAR$  of process  $P_i$  during transaction  $T_r$ . For example,  $AltList_i(T_r)$  is the alternative list of  $P_i$  during transaction  $T_r$ . If significant, the point in time *during* the transaction that is referred to will be stated explicitly.
7. The function  $prev(T_r)$  returns the ID of the transaction executed by the process which immediately preceded  $T_r$ . The existence of  $T_r$  implies the termination of  $prev(T_r)$ . Also,  $prev^0(T_r)$  refers to  $T_r$  itself and  $prev^m(T_r)$  corresponds to the  $m$ th previous transaction entered by  $P_j$ .
8.  $GuardList_i(T_r)$  lists the guards that are passed as parameters to the alternative operation executed by  $P_j$  on transaction  $T_r$ . We will take the liberty of giving *GuardList* a dual meaning — it either refers to a list of *guards* or a list of *processes* that are designated in the I/O commands of these guards. The particular meaning that is intended will be clear from the context.

## 6.2 The Safety Property

Lemmas 1 through 5 lead to theorem 1 which states that no race conditions arise that might cause a process to mistakenly rendezvous with a second process that does not wish to rendezvous with the first. Theorem 2 subsumes theorem 1 and ensures that the algorithm obeys the safety property.

**Lemma 1**  $P_i(T_r)$  signals  $P_j$  iff  $P_i(T_r)$  commits to  $P_j$ .

**Proof:** This follows immediately from examination of the algorithm. A process only sends a signal after it commits, and always sends a signal after it commits. ■

This lemma implies that  $WakeUp_j$  must be set to 0 before a signal can be sent to  $P_j$ . In addition, at most one signal is sent to  $P_j$  each time  $WakeUp_j$  is set to 0.

**Lemma 2** *At the beginning and at the end of each transaction entered by  $P_j$ , the following conditions must hold:*

- (a) *No signals sent to  $P_j$  are pending.*
- (b)  *$WakeUp_j$  is nonzero.*

**Proof:** Use induction on  $m$ , the number of transactions entered by  $P_j$ .

Consider the first transaction ( $m = 1$ ) executed by  $P_j$ .  $WakeUp_j$  is initialized to 1. Because  $WakeUp_j$  can only be set to 0 by  $P_j$  during a transaction,  $WakeUp_j$  must remain nonzero up to at least the beginning of  $P_j$ 's first alternative operation. No process can commit to  $P_j$  until  $WakeUp_j$  becomes 0, so by lemma 1, no signals can be sent to  $P_j$  before its first transaction, and therefore none can be pending. Thus, (a) and (b) are both true at the beginning of  $P_j$ 's first transaction.

During any transaction, and in particular the first,  $P_j$  will either reset  $WakeUp_j$  to 0 exactly once (just before entering the WAITING state), or not at all. If  $P_j$  does not reset  $WakeUp_j$ , then obviously  $WakeUp_j$  is still nonzero at the end of the alternative operation. No signal can be sent to  $P_j$  because no process can commit, so none are pending.

If  $P_j$  does reset  $WakeUp_j$  to 0, then at most one process can commit (and send a signal) to  $P_j$  during this transaction. This is because (1)  $WakeUp_j$  is set to 0 at most one time during this transaction; (2) each process must obtain the lock  $AltLock_j$  before it can examine  $WakeUp_j$  (see the *CheckAndCommit* procedure); (3) as soon as one process reads a zero in  $WakeUp_j$ , it increments it *before* releasing  $AltLock_j$ ; so (4) two processes cannot both read a zero value from  $WakeUp_j$  during a single transaction in  $P_j$ . Because

no two processes can see a zero value in  $WakeUp_j$  during a single transaction, no two processes can commit to  $P_j$  during this (or any) transaction. Therefore, according to lemma 1, at most one signal will be sent to  $P_j$  during this transaction.

$P_j$  always calls *WaitForSignal* after setting  $WakeUp_j$  to zero. Therefore, the only signal that could have been sent to  $P_j$  must have been absorbed by the *WaitForSignal* operation, so none can be pending when the transaction completes (if it completes) satisfying condition (a). Condition (b) must also be satisfied at the end of the transaction because a process must commit *before* sending a signal to  $P_j$ , so  $WakeUp_j$  must be nonzero before the process can resume execution after calling *WaitForSignal*. Therefore, (a) and (b) are again true at the end of the first alternative operation as well as at the beginning.

*Inductive step:* Assume lemma 2 is true on the  $m$ th transaction entered by  $P_j$ . We will now show it is also true on the  $m + 1$ st transaction. According to the inductive hypothesis, no signals are pending at the end of the  $m$ th operation, and  $WakeUp_j$  is nonzero. Therefore, these conditions will remain true until the beginning of the  $m + 1$ st transaction because no process can commit to  $P_j$  until  $WakeUp_j$  becomes 0. As noted in the proof for  $m = 1$ , if (a) and (b) are true at the beginning of any transaction, they will be true at the end of the transaction if it terminates. Therefore, (a) and (b) are true at the end of the  $m + 1$ st transaction entered by  $P_j$ . ■

**Lemma 3** *Two processes,  $P_i$  and  $P_j$ , cannot both commit to a third process  $P_k$  during a single transaction  $T_i$  entered by  $P_k$ .*

This lemma was actually proven as part of the proof of lemma 2, but we include it as a separate lemma for future reference. The proof relies on the fact that  $WakeUp_k$  is not zero at the beginning of the alternative operation and can be set to zero at most one time during a single transaction. The atomicity of the commit operation (i.e., two read-modify-write sequences cannot be inappropriately interleaved) guarantees that only a single process can commit to  $P_k$  during  $T_i$ .

**Lemma 4** *If  $P_i(T_r)$  commits to  $P_j$ , then  $P_j$  must have been in the WAITING state when  $P_i$  committed to  $P_j$ , and  $P_j$  must remain in the WAITING state until  $P_j$  receives the signal sent by  $P_i$  that results from this commitment.*

**Proof:** According to the algorithm,  $P_i$  checks that  $P_j$  is in the WAITING state before trying to commit to  $P_j$ . Let us assume  $P_j$  is in transaction  $T_s$  when  $P_i$  sees  $P_j$  in the WAITING state. Therefore, it only remains to be shown that  $P_j$  is still in the WAITING state when  $P_i$  commits, as well as when the signal is received. This must be the case,

however, because once  $P_j$  enters the `WAITING` state, it cannot change state until it first receives a signal. By lemma 2a, there were no signals pending when transaction  $T_s$  began. By lemma 3 no process other than  $P_i$  will commit to  $P_j$  during this transaction, so no signal other than  $P_i$ 's are sent to, or received by  $P_j$  during this transaction. Therefore,  $P_j$  cannot unblock from the `WaitForSignal` operation and therefore cannot change state until receiving the signal sent by  $P_i$ . ■

The preceding lemma shows that arbitrarily long delays may occur from the time  $P_i$  observes that  $P_j$  is in the `WAITING` state until  $P_i$ 's signal actually arrives at  $P_j$ . If the commit succeeded, this lemma guarantees that nothing “interesting” will happen at  $P_j$  from the time  $P_i$  found it to be waiting until the signal was received.

**Lemma 5** *No signals are lost in the alternative algorithm.*

**Proof:** By lemma 2a, no signals are pending at the beginning of each transaction. By lemma 3, at most one process can commit during a transaction, so at most one signal is sent (and therefore received) during a transaction. Thus, a signal can never arrive during a transaction while another has already been received but is still pending, so no signals are ever lost during a transaction.

No signals destined for a process  $P_j$  are lost between successive transactions of  $P_j$  because none can be sent to  $P_j$  while it is in the `RUNNING` state. This is true because (1) a signal is only sent to  $P_j$  following a commit operation (lemma 1), (2)  $P_j$  must have been in the `WAITING` state when the commit occurred (lemma 4), and (3)  $P_j$  must remain in the `WAITING` state until the signal is received and absorbed by a `WaitForSignal` operation (lemma 4). ■

**Theorem 1** *If  $P_i(T_r)$  signals (rendezvous)  $P_j$ , then  $P_j$  must be in some transaction  $T_s$  both when the signal is sent and when it is received. Further,  $P_j(T_s)$  rendezvous  $P_i(T_r)$ .*

**Proof:** By lemma 4,  $P_j$  must be in a transaction when the signal is sent and when it is received, and remain in the `WAITING` state during this period. By lemma 5,  $P_i$ 's signal cannot be lost. By lemmas 1, 2a and 3, this is the only signal received by  $P_j$  during transaction  $T_s$ , eliminating the possibility of  $P_j$  accepting another signal instead of  $P_i$ 's. Because  $P_j$  always executes `WaitForSignal` when in the `WAITING` state, the signal from  $P_i$  must be received, implying  $P_j$  rendezvous with  $P_i$ . ■

**Theorem 2 (Safety)** *If  $P_i(T_r)$  commits to  $P_j(T_s)$ , then the following properties must be true:*

1. (Mutual consent)  $P_i(T_r)$  rendezvous  $P_j(T_s)$  and  $P_j(T_s)$  rendezvous  $P_i(T_r)$ . In other words, the two communicating parties agree each is rendezvousing with the other.
2.  $P_j \in \text{GuardList}_i(T_r)$  and  $P_i \in \text{GuardList}_j(T_s)$ .
3. Communications between  $P_i(T_r)$  and  $P_j(T_s)$  are compatible.
4.  $P_i$  and  $P_j$  will eventually communicate, complete their transaction, and return to the `RUNNING` state.
5. There does not exist a third process  $P_k$  ( $k \neq i$  and  $k \neq j$ ) such that  $P_k(T_t)$  rendezvous with  $P_i(T_r)$  or  $P_k(T_t)$  rendezvous with  $P_j(T_s)$ .

**Proof:**

1.  $P_i(T_r)$  commits to  $P_j(T_s)$ , implying  $P_i(T_r)$  signals  $P_j(T_s)$  (lemma 1). This in turn implies the mutual rendezvous according to theorem 1.
2. The first part, showing  $P_j \in \text{GuardList}_i(T_r)$ , can be proved by contradiction. Suppose  $P_j \notin \text{GuardList}_i(T_r)$ . Then  $P_i$  would not have committed to  $P_j$  because  $P_i$  only scans those processes in  $\text{GuardList}_i(T_r)$  (see the `FOR` loop in the `TryAlternative` procedure), contradicting our original assumption that  $P_i$  committed to  $P_j$ .

It only remains to be proven that  $P_i \in \text{GuardList}_j(T_s)$ . It is seen from the algorithm that  $P_i$  checks  $\text{AltList}_j$  just before committing to  $P_j$ , and  $\text{AltList}_j$  is set to hold  $\text{GuardList}_j(T_s)$  just before  $P_j$  enters the `WAITING` state, and therefore before the commit. However, an arbitrarily long delay may elapse from the time  $P_i$  checked  $\text{AltList}_j$  to the time it committed. We therefore need to confirm that the value of  $\text{AltList}_j$  that  $P_i$  checked is  $\text{GuardList}_j(T_s)$  rather than  $\text{GuardList}_j(\text{prev}^m(T_s))$  for some  $m > 0$ .

This will be proven by contradiction. Suppose  $P_i$  checked  $\text{GuardList}_j(\text{prev}(T_s))$ . This would imply that the following sequence of events must have occurred:

- (a)  $P_i(T_r)$  checks  $\text{GuardList}_j(\text{prev}(T_s))$  (stored in  $\text{AltList}_j$ );
- (b)  $P_j(T_s)$  modifies  $\text{AltList}_j$  so that it becomes  $\text{GuardList}_j(T_s)$ ;
- (c)  $P_j(T_s)$  sets  $\text{WakeUp}_j(T_s)$  to 0; and
- (d)  $P_i(T_r)$  commits to  $P_j(T_s)$ .

Event (a) must take place by the aforementioned assumption, and event (d) must take place by our original assumption that  $P_i(T_r)$  commits  $P_j(T_s)$ . Event (c) must

precede (d) because  $WakeUp_j(T_s)$  must be reset to 0 before any commitment to  $P_j(T_s)$  can occur (see definition of commit). Event (b) must precede (c) according to the order in which operations are performed in the algorithm. Event (b) must follow (a) in order to satisfy our supposition that  $P_i$  checked  $GuardList_j(prev(T_s))$ . However, this sequence of events is not possible because the locking protocol of the procedure *CheckAndCommit* (used by  $P_i$  when checking  $AltList_j$ ) ensures that  $AltList_j$  is not modified after  $P_i$  checks it (event (a) above), but before  $P_i$  commits (event (d)). Therefore, event (b) could not have occurred between (a) and (d), so our assumption that  $P_i(T_r)$  examined  $GuardList_j(prev(T_s))$  must be incorrect. Similarly, it is not possible that  $P_i(T_r)$  examined  $GuardList_j(prev^m(T_s))$  for any  $m > 0$ .

3. Compatibility is checked when  $P_i(T_r)$  checks that it is in  $AltList_j(T_s)$ . Similarly, this information is implicitly updated whenever  $AltList_j$  is updated. Therefore, this condition is satisfied using the same proof as was used in (2) to show  $P_i$  is in  $GuardList_j(T_s)$ .
4. Once rendezvous occurs between  $P_i(T_r)$  and  $P_j(T_s)$ , each process initiates a communication with the other. Properties (2) and (3) above and the reliability assumption regarding the communication mechanism guarantee that the communication succeeds. Once this occurs, completion of the alternative operation immediately follows.
5. Suppose  $P_k(T_t)$  rendezvoused with either  $P_i(T_r)$  or  $P_j(T_s)$ . Recall a rendezvous occurs by either sending or receiving a signal to or from another process (definition of rendezvous), so there are four possibilities:
  - (a)  $P_k(T_t)$  received a signal from  $P_i(T_r)$ ;
  - (b)  $P_k(T_t)$  received a signal from  $P_j(T_s)$ ;
  - (c)  $P_k(T_t)$  sent a signal to  $P_i(T_r)$ ; or
  - (d)  $P_k(T_t)$  sent a signal to  $P_j(T_s)$ .

We need not consider signals sent before  $T_r$ ,  $T_s$ , or  $T_t$  but received during these respective transactions because none can be pending when the transaction begins (lemma 2a).

- (a) Suppose  $P_k(T_t)$  rendezvoused because it received a signal from  $P_i$  during  $T_r$  (signals generated by  $P_i$  outside  $T_r$  are not relevant). This implies  $P_i(T_r)$  sent signals to *two* processes because our original assumption is that  $P_i(T_r)$  committed

to (and therefore signaled according to lemma 1)  $P_j(T_s)$ . It is clear from the algorithm that a process can signal at most one other process on any given transaction because any time a signal is generated, the transaction always completes without calling the *Signal* procedure again (see figure 4). Therefore,  $P_k(T_t)$  could not have received a signal from  $P_i(T_r)$ .

(b) Suppose  $P_k(T_t)$  received a signal from  $P_j$  during  $T_s$  (signals generated by  $P_j$  outside  $T_s$  are not relevant). This implies  $P_j(T_s)$  both sent a signal to  $P_k$  and received a signal from  $P_i$  within a single transaction. If  $P_j(T_s)$  sent a signal, then, according to the algorithm in figure 4,  $P_j$  must have rendezvoused and completed the transaction without ever entering the WAITING state or setting  $WakeUp_j(T_s)$  to zero. This contradicts our original assumption that  $P_i(T_r)$  committed to  $P_j(T_s)$ .

(c) Suppose  $P_k(T_t)$  signaled  $P_i(T_r)$ . This implies  $P_i(T_r)$  both sent a signal to  $P_j$  and received a signal from  $P_k$  within a single transaction. This latter signal must have been preceded by  $P_k(T_t)$  committing to  $P_i$  (lemma 1). This commit must have occurred during or before  $T_r$ . But,  $P_k(T_t)$  could not have committed to  $P_i$  during  $T_r$  because  $WakeUp_i$  is never equal to zero during  $T_r$ . This is because, by assumption,  $P_i(T_r)$  commits to  $P_j(T_s)$ , so  $P_i(T_r)$  never enters the WAITING state (It is only then that the *WakeUp* variable is set to 0.) Also,  $P_k(T_t)$  could not have committed to  $P_i$  before  $T_r$  and signaled  $P_i$  during  $T_r$  because this would violate lemma 4. Therefore  $P_k(T_t)$  could not have sent a signal to  $P_i(T_r)$ .

(d) Finally,  $P_k(T_t)$  could not have committed (and therefore could not have signaled)  $P_j$  during  $T_s$  because this would imply both  $P_k$  and  $P_i$  committed to  $P_j$  within a single transaction, violating lemma 3.  $P_k(T_t)$  could not have committed to  $P_j$  before  $T_s$  and signaled  $P_j$  during  $T_s$  because this would again violate lemma 4. Thus,  $P_k(T_t)$  could not have signaled  $P_j(T_s)$  either. Therefore,  $P_k(T_t)$  could not have rendezvoused with either  $P_i(T_r)$  or  $P_j(T_s)$ , so the proof is complete. ■

Note from the proof of (2) in the Safety theorem that it is crucial that accesses to *AltList* are controlled by locks, and that the act of checking the *AltList* and committing is atomic to ensure correct operation. Also note that the status of  $P_j$  may change immediately after  $P_i$  checks it. The algorithm operates correctly despite this inconsistency.

### 6.3 The Liveness Property

The liveness property guarantees that no deadlock or livelock situations can arise within the alternative algorithm. Such situations can only be caused by an erroneous *application* program. Lemmas 6



through 11 and theorem 3 prove that the liveness property is maintained by the proposed algorithm.

**Lemma 6** *A process  $P_i$  will never return to the RUNNING state after entering a transaction unless a rendezvous occurred.*

**Proof:** By inspection of the alternative algorithm, the process only returns to the RUNNING state when either: (a)  $P_i(T_r)$  signals  $P_j(T_s)$  or (b) after  $P_i(T_r)$  receives a signal from  $P_j(T_s)$ . In either case,  $P_i(T_r)$  rendezvoused with  $P_j(T_s)$ . ■

**Lemma 7** *A process  $P_i$  cannot remain blocked on a Lock operation in the alternative algorithm for an unbounded amount of time.*

**Proof:** The only *Lock* operation performed by the algorithm is to serialize accesses to *AltList*. However, once any process obtains a lock on any *AltList*, it must eventually release that lock because no unbounded loop or blocking primitive is executed before the corresponding *Unlock* is performed. Therefore, the lock cannot remain in place for an unbounded amount of time. No process will remain blocked attempting to obtain a lock for an unbounded amount of time because every lock will eventually be unlocked, and the the *Lock* primitive is assumed to be fair. ■

**Lemma 8** *Suppose  $P_i \in GuardList_j(T_s)$  and  $P_j \in GuardList_i(T_r)$ , and their respective I/O guards are compatible.  $P_i$  and  $P_j$  cannot both enter the WAITING state during transactions  $T_r$  and  $T_s$ , respectively.*

**Proof:** Proof by contradiction. Suppose both  $P_i$  and  $P_j$  enter the WAITING state on  $T_r$  and  $T_s$ , respectively. Because  $P_i$  reached the WAITING state, it must be the case that the *last* time  $P_i$  scanned the state of  $P_j$  before  $P_i$  entered the WAITING state,  $State_j$  was either (1) RUNNING, (2) SLEEPING, or (3) WAITING but  $P_i$  failed to commit to  $P_j$  (If  $P_i$  successfully committed, they would have rendezvoused and completed the transaction according to theorem 2.) Consider the third case. We will now show that  $P_j$  must have been in a transaction *preceding*  $T_s$  for this case to apply.  $WakeUp_j(T_s)$  is set to 0 *before*  $State_j$  is set to WAITING. Therefore, if  $P_i$  saw  $P_j$  in the WAITING state while  $P_j$  was in transaction  $T_s$ , and  $P_i$  failed when it tried to commit, then it must be that some third process must have committed to  $P_j$  *during*  $T_s$  (after  $WakeUp_j(T_s)$  is set to 0 but before  $P_i$  attempted to commit). But this successful commit must have resulted in a rendezvous, contradicting our original assumption that  $P_j$  blocked indefinitely in the WAITING state while in  $T_s$ . Therefore, if case (3) applies,  $P_j$  must have been in a transaction *previous* to  $T_s$  when  $P_i$  observed it to be in the WAITING state.

Similarly,  $P_j$  also reached the WAITING state, so  $P_i$  must have been in the RUNNING, SLEEPING, or WAITING state for a *previous* transaction the last time  $P_j$  scanned  $P_i$  before  $P_j$  entered the WAITING state.  $P_i$  and  $P_j$  could not have both scanned each other at the same instant because each would have found each other in the ALT state. Therefore, one scanned the other first. Without loss of generality, let us assume  $P_i$  scanned  $P_j$  first.  $P_i(T_r)$  was in the ALT state when it scanned  $P_j$ , and because it did not rendezvous or abort (the latter would require  $P_j$  to be scanned again, making this *not* the last time  $P_i$  scanned  $P_j$ ),  $P_i$  must have remained in the ALT state until it changed to the WAITING state and blocked indefinitely. Therefore, when  $P_j$  later scanned  $P_i$  for the last time,  $P_j$  must have seen  $P_i$  in either the ALT or the WAITING state for transaction  $T_r$ . However, this contradicts the fact that  $P_j$  saw  $P_i$  in the RUNNING, SLEEPING, or WAITING state for a previous transaction. Therefore, the original hypothesis that  $P_i$  and  $P_j$  both entered the WAITING state must be false. ■

**Lemma 9** *A process  $P_i$  cannot remain continuously in the ALT state during a single transaction  $T_r$  for an unbounded amount of time.*

**Proof:** A process remains in the ALT state while it is scanning the processes in its *GuardList* trying to find one which is ready to rendezvous. If none is found, the process proceeds to the WAITING state. Because *GuardList* is necessarily bounded in length, we must show that a process does not spend an unlimited amount of time scanning a particular guard.

$P_i$  moves on to the next *GuardList* entry or eventually changes state when it finds the process corresponding to the current guard is in either the SLEEPING, RUNNING, or WAITING state. Therefore, we only need to consider scanning a process  $P_j$  which is also in the ALT state. If  $TransID_j < TransID_i$ , then  $P_i$  aborts *TryAlternative* and changes to the SLEEPING state. Thus we need only examine the case  $TransID_i < TransID_j$  (both cannot have the same ID). In this case,  $P_i$  enters a loop waiting for  $State_j$  to change. In order for  $P_i$  to remain in this loop an unbounded amount of time,  $P_i$  must continually sample  $P_j$  while  $State_j$  is ALT. There are three ways  $P_i$ 's samples can indicate  $P_j$  remains in the ALT state for an unbounded amount of time: (1)  $P_j$  is also locked into the ALT state for an unbounded amount of time; (2)  $P_j$  repeatedly aborts *TryAlternative*, changes to the SLEEPING state, and then retries *TryAlternative* (changing back to the ALT state) in perfect synchrony with  $P_i$ 's samples of  $State_j$ ; or (3)  $P_j$  repeatedly rendezvous, changes to the RUNNING state, and then initiates a new alternative operation in perfect synchrony with  $P_i$ 's samples of  $State_j$ . These are

exhaustive because a process can only return from *TryAlternative* after a rendezvous or after an aborted attempt. Case (2) cannot occur, however, because the sleep period is set to a time sufficiently large that successive samples by  $P_i$  will detect that  $P_j$  is in the SLEEPING state. Similarly, case (3) cannot occur because the minimum execution time of the *Send* and *Recv* primitives are assumed to be larger than the time between successive samples of the polling loop. Therefore, only case (1) remains.

The previous discussion shows that  $P_i$  can only remain in the ALT state scanning  $P_j$  an unbounded amount of time if the following conditions hold: (1)  $TransID_i < TransID_j$ , and (2)  $P_j$  remains continuously in the ALT state on the same transaction an unbounded amount of time. By the same argument presented above,  $P_j$  will only remain in the ALT state on a single transaction an unbounded amount of time if some other process  $P_k$  is in  $P_j$ 's *GuardList*,  $TransID_j < TransID_k$ , and  $P_k$  remains continuously in the ALT state an unbounded amount of time. Continuing this logic, because the number of processes is bounded, the original process  $P_i$  will only remain in the ALT state for an unbounded time if a *cycle* of processes exists such that each is waiting for the next process in the cycle to leave the ALT state. This would require that  $TransID_i < TransID_j < TransID_k < \dots < TransID_i$ , which is clearly not possible. Therefore, no such cycle can exist, so  $P_i$  cannot remain continually in the ALT state for an unbounded amount of time. ■

**Lemma 10** *The TryAlternative procedure cannot return FAILED an unbounded number of times during a single transaction  $T_r$  in some process  $P_i$ .*

**Proof:** *TryAlternative* returns FAILED if and only if  $P_i$  scans another process  $P_j$  and finds  $P_j$  is also in the ALT state, and  $TransID_j < TransID_i$ . The number of guards in *GuardList* is finite, so if *TryAlternative* fails an unbounded number of times, it must be that for some process  $P_j$ , the conditions  $State_j = \text{ALT}$  and  $TransID_j < TransID_i$  persist for an unbounded amount of time.

$P_j$  cannot remain continually in the ALT state for an unbounded amount of time in a single transaction (lemma 9). Therefore, it must be the case that either (1)  $P_i$  finds  $P_j$  in the ALT state for a *different* transaction an unbounded number of times; or (2) within a single transaction,  $P_j$  repeatedly switches back and forth between the ALT and SLEEPING states for an unbounded number of times, and it so happens that every time  $P_i$  retries *TryAlternative* and scans  $P_j$ ,  $P_i$  finds that  $P_j$  is in the ALT state. In case (2), *TryAlternative* must fail an unbounded number of times in  $P_j$  as well as  $P_i$ .

Case (1): This is not possible because each new transaction ID is larger than all previous IDs. If  $P_i$  finds  $P_j$  in the ALT state for a new transaction an unbounded number of times, this would imply there are an unbounded number of transaction IDs less than  $TransID_i$ . This cannot be the case because transaction IDs are positive integers.

Case (2): An argument similar to that used in lemma 9 can be used here. Summarizing the arguments presented thus far in this lemma, *TryAlternative* in  $P_i$  will only fail an unbounded number of times if it also fails an unbounded number of times in some other process  $P_j$ , where  $TransID_j < TransID_i$ . Similarly,  $P_j$  will only continue to fail if some other process  $P_k$  exists which also continues to fail, and  $TransID_k < TransID_j$ . Because the number of processes is bounded, a cycle of processes must exist such that  $TransID_i > TransID_j > TransID_k > \dots > TransID_i$ , which of course, cannot occur. Therefore, a process cannot fail the *TryAlternative* procedure an unbounded number of times. ■

**Lemma 11** *For each alternative operation initiated by  $P_i$ ,  $P_i$  eventually either rendezvous with some other process  $P_j$  and returns to the RUNNING state, or moves to the WAITING state. In other words, a process cannot remain in the ALT state in the same transaction for an unbounded amount of time.*

**Proof:** The only way a process can *not* reach the WAITING state or rendezvous is to remain continually in the ALT state, or switch back and forth between ALT and SLEEPING an unbounded number of times. The latter case implies *TryAlternative* fails an unbounded number of times within a single transaction. Neither is possible according to lemmas 9 and 10. ■

**Theorem 3 (Liveness)** *Suppose two processes  $P_i$  and  $P_j$  each initiate an alternative operation and  $P_j \in GuardList_i(T_r)$  and  $P_i \in GuardList_j(T_s)$  and their communication requests are compatible. If neither  $P_i$  nor  $P_j$  rendezvous with another process during their respective transactions,  $P_i$  and  $P_j$  will eventually rendezvous with each other during  $T_r$  and  $T_s$ , respectively.*

**Proof:** According to lemma 11,  $P_i$  and  $P_j$  must each eventually either rendezvous or enter the WAITING state. They both cannot enter the WAITING state according to lemma 8. Therefore, at least one of the two processes, say  $P_i$ , must rendezvous. By assumption,  $P_i$  cannot rendezvous with any process other than  $P_j$ , so  $P_i$  must rendezvous with  $P_j$ . By theorem 2,  $P_j$  must also rendezvous with  $P_i$ . Therefore,  $P_i$  and  $P_j$  must eventually rendezvous with each other. ■

## 7 Fairness

One issue regarding the alternative construct that has received considerable attention is *fairness*. In particular, two types of fairness, *weak* and *strong* fairness, have been defined [7,24]. We call an implementation of the alternative construct *weakly fair* if it can be guaranteed that during the infinitely repetitive execution of an alternative command, a guard that remains *continuously* available (i.e., enabled and the neighboring process is ready to communicate) will eventually rendezvous. An implementation is said to be strongly fair if the implementation guarantees that any guard which is available *infinitely often* (though not necessarily continuously as is the case in weak fairness) will eventually rendezvous.

The algorithm shown in figures 2, 3, and 4 is not fair in either the weak or strong sense. However, weak fairness can be achieved by modifying the algorithm so that the order in which the *TryAlternative* procedure scans guards, which implies a certain prioritization of the guards, varies from one call to the next so that each guard is eventually scanned first. More precisely, we modify the algorithm as follows:

- The *Alternative* and *TryAlternative* procedures each receive *all* guards specified in the alternative command as parameters. The original procedures assumed only enabled guards are passed.
- A boolean flag is associated with each guard indicating whether or not it is enabled.
- Define a distinct integer variable for each alternative construct in a given CSP program. These variables could be defined by the compiler. Associate with the *m*th alternative construct in process  $P_i$  the variable  $Alt_{i,m}$ . Initially set to 0, this variable is incremented each time this particular alternative construct is executed. It therefore indicates the number of times  $P_i$  has invoked the corresponding alternative construct.
- The **FOR** loop in the *TryAlternative* procedure is modified so that it begins scanning guard  $(Alt_{i,m} \bmod n) + 1$  rather than the first guard, where  $n$  is the number of guards in the alternative construct. The **FOR** loop is also modified to skip disabled guards. It executes up to  $n$  iterations as before. The index variable of the **FOR** loop “wraps around” to 1 after scanning the *n*th guard.

The modified algorithm is referred to as the *Fair Algorithm*, and is assumed in the discussion which follows.

**Theorem 4 (Fairness)** *Let  $P_i$  be blocked on an alternative operation (i.e.,  $P_i$  is in the WAITING state) in which some process  $P_j$  is listed in some enabled guard. Further, let us assume  $P_i$  does not become unblocked through a rendezvous with any process other than  $P_j$ . Consider an alternative construct  $A$  in  $P_j$  that has been executed  $m$  times and contains  $n$  guards, one of which ( $g_v$ ) contains a compatible communication with  $P_i$ . If  $P_j$  now executes  $A$  at least  $n$  more times and  $g_v$  is enabled on each of these  $n$  invocations of  $A$ , then  $P_i$  and  $P_j$  will rendezvous before the  $(m + n)$ th execution of  $A$  completes.*

**Proof:** The theorem can be proved by contradiction. Assume  $P_i$  does not rendezvous with  $P_j$  before the  $(m + n)$ th execution of  $A$ . For this to happen,  $P_j$  must continually be rendezvousing with some other process(es) before it scans  $P_i$ , because the moment it scans  $P_i$ , it will see that  $P_i$  is in the WAITING state and rendezvous with  $P_i$ . However, the *Fair Algorithm* guarantees that within  $n$  executions of  $A$ ,  $g_v$  will become the *first* guard that is scanned. When  $g_v$  is scanned first, no other process can rendezvous with  $P_j$  before  $P_j$  scans  $P_i$ , so a rendezvous between  $P_i$  and  $P_j$  must take place. ■

The following corollary follows immediately from this theorem:

**Corollary 1** *In an infinitely repetitive execution of an alternative construct, a guard cannot remain continually available for an unbounded amount of time without eventually rendezvousing.*

This shows that the *Fair Algorithm* is weakly fair. It demonstrates, for instance, that a process waiting to be served by another process cannot be continuously denied service for an unbounded amount of time. The *Fair Algorithm* is *not* strongly fair, however. Modification of this algorithm to one which is strongly fair is an open question. None of the alternative algorithms that have been developed thus far (based on message-passing architectures) is strongly fair.

## 8 Conclusions

We have presented an algorithm that implements the generalized alternative construct in CSP. Unlike previous algorithms, this is based on a shared memory architecture. It has been shown that the algorithm maintains the safety and liveness properties required by any correct implementation. Extensions to the algorithm that allow processes to terminate and guarantee weak fairness were also presented. An implementation, written in C, has been developed for a 16-processor BBN Butterfly parallel processor. Empirical performance evaluation of this implementation is in progress.

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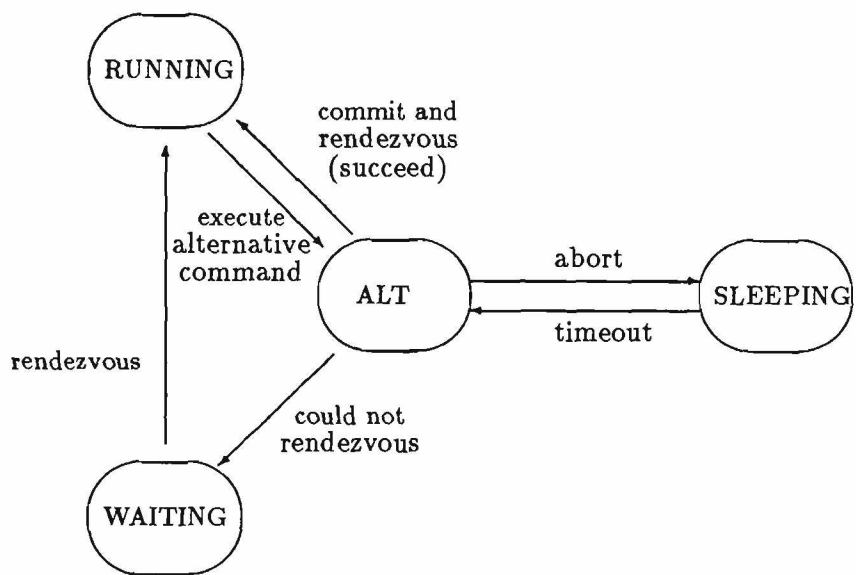


Figure 1: The State diagram of a process.

```

/* r is the remote process */
PROCEDURE CheckAndCommit(AltListr, gi): INTEGER;
VAR
    INTEGER GuardNumber; /* number of matching guard */
BEGIN
    Lock(AltLockr);
    /* check guard matches and is compatible */
    GuardNumber := CheckGuard(AltListr, gi);
    IF (GuardNumber = FAILED) THEN
        Unlock(AltLockr);
        RETURN (FAILED);
    /* try to commit */
    ELSEIF (WakeUpr = 0) THEN
        WakeUpr = WakeUpr + 1;
        Unlock(AltLockr);
        RETURN (GuardNumber);
    ELSE
        Unlock(AltLockr);
        RETURN (FAILED);
    END;
END CheckAndCommit;

```

Figure 2: Procedure to check that a potential communication is valid and, if so, to commit. The *CheckGuard* function returns the number of a matching (and compatible) remote guard or returns FAILED if none was found.

```

/* gi are enabled I/O guards */
PROCEDURE Alternative(g1, ..., gn): INTEGER;
VAR
  INTEGER ReturnValue; /* indicates guard that rendezvoused */
BEGIN
  /* l is the local process id */
  TransIDl := AtomicAdd(NextTransID);
  ReturnValue := FAILED;
  WHILE (ReturnValue = FAILED) DO
    ReturnValue := TryAlternative(g1, ..., gn);
    IF (ReturnValue = FAILED) THEN Sleep(TimeOut); END;
  END;
  RETURN (ReturnValue);
END Alternative;

```

Figure 3: The “front end” procedure. *TryAlternative* returns the number of the guard on which a rendezvous took place or FAILED if it aborted.

```

PROCEDURE TryAlternative( $g_1, \dots, g_n$ ): INTEGER;
VAR
  BOOLEAN flag;
  INTEGER GuardNumber; /* corresponding guard of  $P_r$  */
  INTEGER i, r;
BEGIN
  State1 := ALT;
  /* look for rendezvous with a waiting process. */
  FOR i:=1 TO n DO
    r := CommunicantID( $g_i$ );
    flag := TRUE;
    WHILE (flag) DO
      CASE Stater DO /* The remote process state. */
        RUNNING: flag := FALSE;
        SLEEPING: flag := FALSE; /* try next guard */
        WAITING: GuardNumber := CheckAndCommit(AltListr,  $g_i$ );
          IF (GuardNumber = FAILED) THEN
            flag := FALSE; /* try next guard */
          ELSE /* Wake up  $P_r$  */
            State1 := RUNNING;
            Signal(r, GuardNumber);
            Communicate( $g_i$ );
            RETURN (i);
          END;
        ALT: IF (TransID1 < TransIDr) THEN
          WHILE (Stater = ALT) DO END;
        ELSE /* busy wait loop. */
          State1 := SLEEPING;
          RETURN (FAILED); /* abort...*/
        END; /* if-then-else */
      END; /* case statement */
    END; /* while loop */
  END; /* for statement */
  /* couldn't find guard to rendezvous */
  Lock(AltLock1); AltList1 := ( $g_1, \dots, g_n$ ); Unlock(AltLock1);
  WakeUp1 := 0; /* first to commit gets rendezvous */
  State1 := WAITING;
  i := WaitForSignal(); /* Blocks */
  State1 := RUNNING;
  Communicate( $g_i$ )
  RETURN (i);
END TryAlternative;

```

Figure 4: The *TryAlternative* procedure attempts to rendezvous with a process listed in an I/O guard, and does not return until rendezvous takes place.